

Mathematics

Goal: The Real and Complex Number Systems

RIT Score Range:211 - 220Statements Last Updated:Mar 10, 2014

Skills and Concepts to Enhance (73% Probability*) 201 - 210	Skills and Concepts to Develop (50% Probability*) 211 - 220	Skills and Concepts to Introduce (27% Probability*) 221 - 230
Ratios and Proportional Relationships	Ratios and Proportional Relationships	Ratios and Proportional Relationships
Converts between inches and feet	 Solves problems involving equivalent fractions 	Solves real-world problems involving decimals (not money) using
 Solves simple problems involving measurement of length 	Solves 1-step problems involving proportions	multiplication
• Estimates simple conversions involving length between the customary	• Calculates basic percents of a number (e.g., 10%, 20%, 25%, 50%,	Solves problems involving ratios
and metric system	100%)	Solves 1-step problems involving proportions
 Converts between cups and pints 	Converts between inches and feet	• Calculates basic percents of a number (e.g., 10%, 20%, 25%, 50%,
 Converts between cups, pints, and quarts 	 Converts between inches, feet, and yards 	100%
 Computes simple conversions among units of time (hours, days) 	 Solves simple problems involving measurement of length 	• Calculates a percent of a number (e.g., 6% of 30)
 Computes more difficult conversions among units of time 	 Converts between cups, pints, quarts, and gallons 	• Calculates a number from a percent (e.g., 4 is 9% of what)
 Applies dimensional analysis to simple real-world problems (time) 	Apply dimensional analysis to simple real-world problems (capacity)	Solves problems involving percents
 Solves simple problems involving miles per gallon 	 Computes more difficult conversions among units of time 	Solves problems involving tax and tips
 Solves simple problems involving miles/kilometers per hour 	Applies dimensional analysis to simple real-world problems (time)	Converts between inches, feet, and yards
Determines unit price	 Solves simple problems involving miles per gallon 	• Converts between millimeters, centimeters, meters, and kilometers
 Writes the missing number in a proportion using basic facts 	Determines unit price	Uses dimensional analysis for unit conversions (length)
 Identifies the percent represented in a 2-D region 	Solves problems involving rates	Solves problems involving length in the customary system and converts to larger or smaller units
	• Writes a basic percent as a fraction and vice versa (e.g., 10%, 25%, 50%, 100%)	Converts between ounces and pounds
	• Expresses a percent as a fraction with 100 as the denominator and	Converts between ounces, pounds, and tons
	vice versa	Converts between cups, pints, quarts, and gallons
	 Recognizes and writes proportions 	Converts within the metric system
	 Identifies the percent represented in a 2-D region 	Apply dimensional analysis to simple real-world problems (capacity)
		Solves problems involving capacity in the customary system and converts to larger or smaller units
		Computes 2-step conversions between units of time
		Applies dimensional analysis to simple real-world problems (time)
		Solves complex problems involving miles per gallon
		Solves complex problems involving miles/kilometers per hour
		Solves problems involving rates
		Solves problems involving perimeter and converts to larger or smaller units
		• Interprets data given in circle graphs to solve complex problems (with percents)
		Expresses a percent as a fraction and vice versa
		Writes a ratio as a percent and vice versa
		Uses concrete and pictorial models to represent ratios
		• Writes the missing number in a proportion with numbers other than basic facts (e.g., 5/13=?/117)

Explanatory Notes



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• Multiplies a fraction by a whole number

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Perform Operations	Perform Operations	Perform Operations
 Uses rounding to estimate answers to real-world problems involving numbers 1000 or greater with addition and subtraction (whole numbers only) 	 Uses rounding to estimate answers to real-world problems involving multiplication and division of numbers less than 100 (whole numbers only) 	 Uses rounding to estimate answers to real-world problems involving multiplication and division of numbers less than 100 (whole numbers only)
 Uses rounding to estimate answers to addition and subtraction problems (whole numbers only) 	Uses rounding to estimate answers to real-world problems involving numbers less than 1000 with multiplication and division (whole numbers are being the set of t	• Uses rounding to estimate answers to real-world problems involving numbers less than 1000 with multiplication and division (whole numbers
 Adds multiple-digit numbers, with regrouping, with sums over 1000 		only)
 Adds multiple-digit numbers with sums under 1000 	Uses rounding to estimate answers to real-world problems involving numbers 1000 or greater using multiplication and division (whole	Uses rounding to estimate answers to real-world problems involving numbers 1000 or greater using multiplication and division (whole
 Performs mental computation with more than 4 addends 	numbers only)	numbers only)
 Subtracts 3- or 4-digit numbers with regrouping 	Uses rounding to estimate answers to difficult multiplication and	Multiplies multiple-digit numbers
 Subtracts numbers with 5 digits or more with regrouping 	division problems (whole numbers only)	Divides a 4-digit number by a 2-digit number
Solves real-world whole number problems involving subtraction with	 Subtracts numbers with 5 digits or more with regrouping 	Divides multiple-digit numbers
numbers 100 and under (analysis)	 Instantly recalls basic multiplication and division facts in a table 	Solves complex word problems involving whole number division with
 Solves problems using the inverse relationship between addition and subtraction 	 Multiplies a 2-digit number by a 2-digit number with regrouping 	remainder (e.g., 2-step, 2-digit divisor)
Instantly recalls basic multiplication and division facts in a table	 Multiplies a 3-digit number by a 2-digit number with regrouping 	Solves real-world multiple-step problems involving whole numbers
Multiplies a 2-digit number by a 1-digit number with regrouping	 Performs mental computation with multiplication 	 Demonstrates an understanding of multiple properties
Multiplies a 3- or 4-digit number by a 1-digit number	 Uses multiplication strategies to explain computation (e.g., doubles, 9- patterns, decomposing, partial products) 	Adds fractions with like denominators with reducing or converting to a mixed fraction
 Multiplies multiple 1-digit numbers 	Multiplies a 3-digit number by a 3-digit number	Adds fractions with unlike denominators without reducing
 Multiplies a 2-digit number by a 2-digit number with regrouping 	Multiplies a 4- or more digit number by multiples of 100 or 1000	Adds fractions with unlike denominators with reducing or converting to
 Multiplies a 3-digit number by a 2-digit number with regrouping 	Multiplies multiple-digit numbers	a mixed fraction
 Performs mental computation with multiplication 	Models whole number multiplication and division algorithms (e.g., uses	• Adds simple mixed fractions with unlike denominators (e.g., halves,
 Multiplies a 2- or 3-digit number by multiples of 10 or 100 	physical materials to show 4 groups of 3 objects)	thirds, fourths, eighths)
Multiplies a 3-digit number by a 3-digit number	Divides a 2-digit number or a 3-digit number by a 1-digit number with a remainder	 Adds mixed fractions where converting from improper fractions is necessary
 Solves word problems involving whole number multiplication with numbers greater than 10 x 10 	Performs mental computation with division	Subtracts fractions with like denominators with reducing
Models whole number multiplication and division algorithms (e.g., uses	Divides a 4-digit number by a 1-digit number with no remainder	Subtracts fractions with unlike denominators without reducing
physical materials to show 4 groups of 3 objects)	Divides a 3-digit number by a 2-digit number	Subtracts fractions with unlike denominators with reducing
 Instantly recalls division facts with dividend and divisors less than 13 	Divides a 4-digit number by a 2-digit number	• Subtracts mixed fractions with unlike denominators with no regrouping
Divides a 2-digit number by a 1-digit number with no remainder	Divides multiple-digit numbers	 Subtracts whole numbers, fractions, and mixed fractions
Divides a 2-digit number or a 3-digit number by a 1-digit number with a remainder	Solves whole number word problems with division over 10 x 10	Subtracts whole numbers, fractions, and mixed fractions with regrouping
Performs mental computation with division	Solves complex word problems involving whole number division with remainder (e.g., 2-step, 2-digit divisor)	Solves real-world problems involving addition and subtraction of
Divides a 3-digit number by a 1-digit number with no remainder	Solves real-world problems involving 2-step multiple operations, whole	fractions where converting one denominator is necessary
 Divides a 4-digit number by a 1-digit number with no remainder 	numbers only	Uses models to multiply and divide fractions and connect the actions
 Divides a 3-digit number by a multiple of 10 	Solves real-world multiple-step problems involving whole numbers	Nultiplice of rection by a fraction without reducing to airpalact form
Divides a 4-digit number by a 2-digit number	Demonstrates an understanding of the inverse relationship between	(complex problem)
 Solves word problems with whole number division facts with dividend and divisors less than 11 	Adds fractions with like denominators without reducing	Multiplies a fraction by a fraction where reducing to simplest form is necessary

* At the range mid-point, this is the probability students would correctly answer items measuring these concepts and skills. Both data from test items and review by NWEA curriculum specialists are used to place Learning Continuum statements into appropriate RIT ranges. Blank cells indicate data are limited or unavailable for this range or document version.

Explanatory Notes



Mathematics

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Skills and Concepts to Enhance (73% Probability*) 201 - 210	Skills and Concepts to Develop (50% Probability*) 211 - 220	Skills and Concepts to Introduce (27% Probability*) 221 - 230
Perform Operations	Perform Operations	Perform Operations
 Solves simple word problems involving whole number division with remainder (e.g., 1-step, 1-digit divisor) 	Adds fractions with like denominators with reducing or converting to a mixed fraction	Multiplies mixed fractions
• Solves whole number word problems with division over 10 x 10	Adds fractions with unlike denominators without reducing	Divides a fraction by a fraction
• Determines the remainder in a real-world problem (whole numbers)	Adds simple mixed fractions with unlike denominators (e.g., halves	Divides a mixed fraction by a fraction
Uses division for multiple-step real-world problems (whole numbers)	thirds, fourths, eighths)	Solves 1-step real-world problems involving fractions with multiplication and division
Solves real-world problems involving 2-step multiple operations, whole numbers only	Subtracts simple fractions with unlike denominators without reducing (e.g., halves, quarters, thirds, eighths)	Solves 2- or more step real-world problems involving fractions with multiplication and division
 Adds fractions with like denominators without reducing 	 Subtracts fractions with unlike denominators without reducing 	Solves problems involving fractions (e.g., multiple operations,
Adds whole numbers and fractions	 Subtracts mixed fractions with like denominators with no regrouping 	conversions)
Uses models to add and subtract fractions and connect the actions to	Subtracts mixed fractions with unlike denominators with no regrouping	Adds decimals to the hundredths place in horizontal format (not same number of digite)
algorithms	Solves real-world problems involving addition and subtraction of fractions where converting one dependienter is percenter.	Adda dasimple through the hundred the user dthe place
 Subtracts fractions with like denominators without reducing 	a Liese models to multiply and divide fractions and connect the actions	Adds decimals through the hundred the place (not some number of
Subtracts mixed fractions with like denominators with no regrouping	to algorithms	digits)
 Solves real-world 1-step problems involving addition and subtraction of fractions with like denominators Multiples of fraction without reducing to simplest form 	Multiplies a fraction by a fraction where reducing to simplest form is necessary	Subtracts decimals to the thousandths place, horizontally, with and without regrouping
 Multiplies a fraction by a fraction without reducing to simplest form (simple problem) 	Multiplies a fraction by a whole number	Subtracts decimals through the hundred-thousandths place,
Adds decimals to the thousandths place horizontally with and without regrouping	 Solves 1-step real-world problems involving fractions with multiplication and division 	 horizontally Subtracts a decimal from a whole number, horizontally
Subtracts decimals to the hundredths place (same number of digits) with regrouping	Adds decimals to the hundredths place in horizontal format (not same number of digits)	Multiplies a decimal by a decimal, vertical form (factors to tenths or hundredths)
Subtracts decimals to the thousandths place, vertically, with and without reasoning	Adds decimals to the thousandths place horizontally with and without regrouping	Multiplies a decimal by a decimal (factors to hundredths)
Subtracts desimals through the hundred theusandthe place vertically	Adds decimals through the hundred-thousandths place	• Multiplies a decimal by a decimal (factors to thousand the)
Computer the value of multiple hills and coins (addition/subtraction	Subtracts decimals to the thousandths place, horizontally, with and	Multiplies a decimal by a decimal (lactors to thousandins)
only)	without regrouping	Divides a decimal by 10, 100, 1000
Multiplies a decimal by whole number	Computes the value of multiple bills and coins (addition/subtraction	Computes with dollars and conts over \$5.00 and converts to decimals
Divides decimal by a whole number	only)	(multiplication/division)
• Computes with dollars and cents up to and including \$5.00 and	money over \$5.00 (addition/subtraction only)	Computes the value of multiple bills and coins (multiplication/division)
Computer addition and subtraction on multiple stop real world	Multiplies a decimal by a decimal, vertical form (factors to tenths or	Calculate the sum of integers using a number line
problems involving money	hundredths)	Adds integers with unlike signs
Computes money problems with multiple operations (addition/	Multiplies a decimal by a decimal (factors to hundredths)	Adds several positive and negative integers
subtraction only)	Divides decimal by a whole number	Uses models to add and subtract integers and connect the actions to algorithms
Computes addition, subtraction, multiplication, and division on multiple- step, real-world problems involving money	 Analyzes and computes 1 operation on real-world problems involving money over \$5.00 (multiplication/division) 	Subtracts integers
 Solves real-world problems involving addition and subtraction of integers 	Computes with dollars and cents over \$5.00 and converts to decimals (multiplication/division)	Solves real-world problems involving addition and subtraction of integers
 Solves problems involving measurement of time 	Computes addition and subtraction on multiple-step real-world	Solves problems involving addition and subtraction of integers
Solves simple problems involving elapsed time, with the conversion of	problems involving money	Multiplies integers with unlike signs
hours		Divides integers with unlike signs

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Perform Operations	Perform Operations	Perform Operations
 Solves problems using tables 	• Computes addition, subtraction, multiplication, and division on multiple-	Divides integers with like signs
Writes a terminating decimal as a fraction or mixed number	step, real-world problems involving money	 Adds rational expressions in decimal form
• Expresses the equivalent form of a fraction, decimal, and/or percent	 Adds integers with like signs 	 Identifies the additive inverse property
(simple fraction)	 Uses models to add and subtract integers and connect the actions to algorithms 	Solves difficult problems involving elapsed time, with the conversion of hours
	 Solves real-world problems involving addition and subtraction of integers 	Interprets data given in tables to solve problems
	Multiplies integers with unlike signs	Writes a simple mixed fraction as a decimal and vice versa
	Divides integers with unlike signs	 Writes a fraction or mixed number as a decimal when the denominator is a multiple of 10
	Divides integers with like signs	Determines factors of whole numbers
	• Demonstrates an understanding that division by 0 is undefined	Uses multiple number theory concepts to solve problems (e.g., factors,
	• Solves difficult problems involving elapsed time, with the conversion of	digits, odd/even, divisibility)
	hours	 Uses factor and multiple concepts to solve simple problems
	 Selects and uses the appropriate units depending on degree of accuracy required to solve problems 	 Identifies common factors of two or more numbers
	• Expresses a simple fraction as a decimal	 Identifies the greatest common factor of whole numbers
	Writes a simple mixed fraction as a decimal and vice versa	
	Writes a fraction or mixed number as a decimal when the denominator is a multiple of 10	
	 Expresses a percent as a decimal and vice versa 	
	 Expresses the equivalent form of a fraction, decimal, and/or percent (simple fraction) 	
	Determines factors of whole numbers	
	Identifies numbers as prime	
	 Identifies common factors of two or more numbers 	
	 Identifies the greatest common factor of whole numbers 	
Extend and Use Properties	Extend and Use Properties	Extend and Use Properties
 Graphs ordered pairs in the first quadrant 	• Predicts the relative size of the answer when computing with 10's,	 Graphs ordered pairs in all quadrants
 Determines and names locations in the first quadrant on a labeled grid or coordinate system (e.g., map or graph) 	100's, 1000's Predicts the relative size of the answer when multiplying whole	 Computes and interprets distance, given a set of ordered pairs (horizontal and vertical lines)
Determines the distance between horizontal and vertical lines in the	numbers	Determines the relative magnitude of whole numbers
first quadrant of a rectangular coordinate system	• Determines the distance between horizontal and vertical lines in the	Rounds whole numbers to the nearest million
 Determines the distance between points, following grid lines, in the first quadrant on a coordinate graph (as in city blocks) 	 Irst quadrant of a rectangular coordinate system Locates the origin on a coordinate grid 	• Writes equivalent forms of whole numbers using place value (numbers 100 or greater) (e.g. $253 - 2$ hundreds 5 tens and 3 ones)
 Locates the origin on a coordinate grid 	• Rounds 4-, 5-, and 6-digit whole numbers to the nearest hundred	Writes whole numbers in standard and exponential form
 Identifies whole numbers over 999 using base-10 blocks 	• Rounds 4-, 5-, and 6-digit whole numbers to the nearest thousand	Identifies a fractions in lowest terms from a region or set
• Identifies the numeral and written name for whole numbers with a zero	• Rounds 4-, 5-, and 6-digit whole numbers to the nearest ten thousand	Determines simple equivalent fractions using multiples
between digits to the ten thousands place	Rounds wholes numbers to the nearest billion	Determines equivalent fractions using multiples
 Identifies the numeral and written name for whole numbers over 100,000 		Compares fractions (e.g., comparing numerators and denominators)

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Extend and Use Properties	Extend and Use Properties	Extend and Use Properties
• Compares whole numbers through the billions using the symbols <, >, or =	Writes whole numbers in standard and expanded form through the hundred thousands	Uses alternative algorithms to explain the meaning of fraction Papresents a decimal to thousandths place (e.g., three thousandths =
 Orders whole numbers a million or greater using < or > symbols 	 Identifies equivalent fractions using visual representations 	
 Rounds 4-, 5-, and 6-digit whole numbers to the nearest ten 	 Identifies a fractions in lowest terms from a region or set 	• Represents a decimal to the hundred thousandths place - (e.g., three
 Rounds 4-, 5-, and 6-digit whole numbers to the nearest hundred 	 Identifies eighths, reduced to lowest terms, from a region or set 	hundred thousandths = 0. 00003)
 Rounds 4-, 5-, and 6-digit whole numbers to the nearest thousand 	 Determines simple equivalent fractions using multiples 	Writes a decimal for a shaded region to the hundredths place
 Rounds whole numbers to the nearest hundred thousand 	 Converts fractions to lowest terms 	Compares and orders decimals to the hundredths place (not same number of digits after decimal)
 Rounds wholes numbers to the nearest billion 	• Writes mixed numbers as improper fractions and improper fractions as	Compares and orders desimals to the theusandthe place (not same)
 Explains the rules for rounding 	mixed numbers	number of digits after decimal)
• Writes equivalent forms of whole numbers using place value (e.g., 54	Compares fractions on a number line	Compares and orders decimals past the thousandths place
= 4 tens and 14 ones)	Compares fractions greater than or less than a given fraction using visual representations	Rounds decimals to the nearest hundredth
 Identifies the place value and value of each digit in whole numbers through the billions 	Compares fractions and mixed numbers	Rounds decimals to nearest thousandth
Writes whole numbers in standard and expanded form through the	Compares fractions and mixed numbers using symbols	• Identifies the place value and value of each digit to the hundredths and
hundred thousands	Orders fractions on a number line	thousandths
 Applies base ten place value concepts with whole numbers to solve problems 	 Explains different interpretations of fractions (e.g., parts of a whole, parts of a set, and division of whole numbers by whole numbers) 	Applies base ten place value concepts to solve problems using decimals
 Writes whole numbers using place value terms and vice versa 	Represents a decimal to the hundredths place (e.g., three hundredths	Compares two integers
 Identifies halves of a region using nonadjacent parts 	= 0.03)	Orders integers on a number line
 Identifies equivalent fractions using visual representations 	 Compares and orders decimals past the thousandths place 	Orders integers
 Expresses 1 in many different ways (e.g., 3/3, 4/4) 	 Rounds decimals to the nearest whole number 	Locates rational numbers on a number line
 Converts a basic fractional numeral to lowest terms (e.g., halves, thirds, quarters) 	Rounds decimals to the nearest tenth Applies base ten place value concepts to solve problems using	 Orders rational numbers, in a/b form Orders fractions and decimals to the hundred thousandths
Writes mixed numbers as improper fractions and improper fractions as mixed numbers	decimals Identifies an integer from a number line 	
• Compares fractions (e.g., common denominator, 1 in the numerator, denominator is 2, 3, 4, 6, 8, 10)	Compares two integers	
Orders fractions on a number line	• Orders integers on a number line	
 Explains different interpretations of fractions (e.g., parts of a whole, parts of a set, and division of whole numbers by whole numbers) 	Defines integers	
 Identifies a decimal on a number line to the tenths place 		
 Rounds decimals to the nearest whole number 		
 Compares integers on a number line 		
New Vocabulary: biggest, coordinate, coordinate point, expanded numeral, larger, miles per gallon, origin	New Vocabulary: century, coin, common factor, decimal form, greatest common factor, how long, lowest term, lowest terms, reduce, triple	New Vocabulary: real number, ten million
New Signs and Symbols: ft feet, in. inch, mpg miles per gallon, - negative number	New Signs and Symbols: \$ dollar sign, hr hour, kg kilogram, - negative sign, ≠ not equal to, yd yard	centimeter/centimetre, °C degrees Celsius, km kilometer/kilometre, mL milliliter/milliliter, # number, / per, + positive number, : ratio

Explanatory Notes