

Mathematics

Goal: The Real and Complex Number Systems

RIT Score Range:221 - 230Statements Last Updated:Mar 10, 2014

Skills and Concepts to Enhance (73% Probability*) 211 - 220	Skills and Concepts to Develop (50% Probability*) 221 - 230	Skills and Concepts to Introduce (27% Probability*) 231 - 240
Ratios and Proportional Relationships	Ratios and Proportional Relationships	Ratios and Proportional Relationships
<ul> <li>Solves problems involving equivalent fractions</li> </ul>	Solves real-world problems involving decimals (not money) using	Uses estimation to solve problems involving proportional reasoning
<ul> <li>Solves 1-step problems involving proportions</li> </ul>	multiplication	(decimals only)
<ul> <li>Calculates basic percents of a number (e.g., 10%, 20%, 25%, 50%, 100%)</li> </ul>	<ul> <li>Solves problems involving ratios</li> <li>Solves 1-step problems involving proportions</li> </ul>	Solves real-world problems involving decimals (not money) using multiplication
Converts between inches and feet	Calculates basic percents of a number (e.g., 10%, 20%, 25%, 50%,	Solves problems involving equivalent fractions (analysis)
Converts between inches, feet, and yards	100%)	Solves problems involving ratios
Solves simple problems involving measurement of length	Calculates a percent of a number (e.g., 6% of 30)	<ul> <li>Solves multiple-step problems involving proportions</li> </ul>
Converts between cups, pints, quarts, and gallons	Calculates a number from a percent (e.g., 4 is 9% of what)	Calculates a percent of a number (e.g., 6% of 30)
Apply dimensional analysis to simple real-world problems (capacity)	Solves problems involving percents	• Calculates the percent one number is of another (e.g., 20 is what % of
Computes more difficult conversions among units of time	Solves problems involving tax and tips	90)
Applies dimensional analysis to simple real-world problems (time)	Converts between inches, feet, and yards	Solves problems involving percents
Solves simple problems involving miles per gallon	Converts between millimeters, centimeters, meters, and kilometers	Solves problems involving percents (analysis)
Determines unit price	Uses dimensional analysis for unit conversions (length)	<ul> <li>Solves problems involving simple percent discounts (e.g., finding sale price)</li> </ul>
<ul> <li>Solves problems involving rates</li> </ul>	Solves problems involving length in the customary system and converts to larger or smaller units	Solves problems involving percent increase and decrease
• Writes a basic percent as a fraction and vice versa (e.g., 10%, 25%,	Converts between ounces and pounds	<ul> <li>Solves problems involving tax and tips</li> </ul>
50%, 100%)	Converts between ounces, pounds, and tons	<ul> <li>Calculates commission/deductions and total pay</li> </ul>
<ul> <li>Expresses a percent as a fraction with 100 as the denominator and vice versa</li> </ul>	Converts between cups, pints, guarts, and gallons	Converts between millimeters, centimeters, meters, and kilometers
<ul> <li>Recognizes and writes proportions</li> </ul>	Converts within the metric system	<ul> <li>Uses dimensional analysis for unit conversions (length)</li> </ul>
<ul> <li>Identifies the percent represented in a 2-D region</li> </ul>	Apply dimensional analysis to simple real-world problems (capacity)	• Converts between the customary and metric system given conversion ratios (2-step, length)
	Solves problems involving capacity in the customary system and converts to larger or smaller units	Apply dimensional analysis to simple real-world problems (length)
	Computes 2-step conversions between units of time	<ul> <li>Solves problems involving length in the customary system and converts to larger or smaller units</li> </ul>
	Applies dimensional analysis to simple real-world problems (time)	Converts between grams and kilograms
	<ul> <li>Solves complex problems involving miles per gallon</li> </ul>	Solver's between grains and kingrains     Solves problems involving weight in the customary system and
	Solves complex problems involving miles/kilometers per hour	converts to larger or smaller units
	Solves problems involving rates	Converts within the metric system
	Solves problems involving perimeter and converts to larger or smaller	Apply dimensional analysis to simple real-world problems (capacity)
	<ul><li>units</li><li>Interprets data given in circle graphs to solve complex problems (with</li></ul>	<ul> <li>Solves problems involving capacity in the customary system and converts to larger or smaller units</li> </ul>
	percents)	<ul> <li>Solves complex problems involving miles per gallon</li> </ul>
	Expresses a percent as a fraction and vice versa	Solves problems comparing unit prices
	Writes a ratio as a percent and vice versa	Solves problems involving rates
	Uses concrete and pictorial models to represent ratios	Interprets data given in circle graphs to solve complex problems (with
	• Writes the missing number in a proportion with numbers other than basic facts (e.g., 5/13=?/117)	percents)
		• Expresses a percent as a fraction and vice versa
		Writes a ratio as a percent and vice versa
		Identifies the ratio from a given real-world situation

#### **Explanatory Notes**



### Mathematics

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Skills and Concepts to Enhance (73% Probability*) 211 - 220	Skills and Concepts to Develop (50% Probability*) 221 - 230	Skills and Concepts to Introduce (27% Probability*) 231 - 240
Perform Operations	Perform Operations	Perform Operations
<ul> <li>Uses rounding to estimate answers to real-world problems involving</li> </ul>	Uses rounding to estimate answers to real-world problems involving	Divides multiple-digit numbers
multiplication and division of numbers less than 100 (whole numbers	multiplication and division of numbers less than 100 (whole numbers only)	Divides numbers by powers of 10
only)  • Uses rounding to estimate answers to real-world problems involving  with multiplication and division (whole numbers)	Uses rounding to estimate answers to real-world problems involving	Adds fractions with unlike denominators with reducing or converting to     a mixed fraction
numbers less than 1000 with multiplication and division (whole numbers only)	numbers less than 1000 with multiplication and division (whole numbers only)	Adds simple mixed fractions with unlike denominators (e.g., halves, thirds, fourths, eighths)
<ul> <li>Uses rounding to estimate answers to real-world problems involving numbers 1000 or greater using multiplication and division (whole numbers only)</li> </ul>	Uses rounding to estimate answers to real-world problems involving numbers 1000 or greater using multiplication and division (whole numbers only)	Adds mixed fractions where converting from improper fractions is necessary
<ul> <li>Uses rounding to estimate answers to difficult multiplication and</li> </ul>	Multiplies multiple-digit numbers	Subtracts whole numbers, fractions, and mixed fractions
division problems (whole numbers only)	Divides a 4-digit number by a 2-digit number	Subtracts whole numbers, fractions, and mixed fractions with
<ul> <li>Subtracts numbers with 5 digits or more with regrouping</li> </ul>	Divides multiple-digit numbers	regrouping
<ul> <li>Instantly recalls basic multiplication and division facts in a table</li> </ul>	Solves complex word problems involving whole number division with	Solves real-world problems involving addition and subtraction of fractions where converting both denominators is necessary
<ul> <li>Multiplies a 2-digit number by a 2-digit number with regrouping</li> </ul>	remainder (e.g., 2-step, 2-digit divisor)	Uses models to multiply and divide fractions and connect the actions
<ul> <li>Multiplies a 3-digit number by a 2-digit number with regrouping</li> </ul>	Solves real-world multiple-step problems involving whole numbers	to algorithms
<ul> <li>Performs mental computation with multiplication</li> </ul>	Demonstrates an understanding of multiple properties	Multiplies mixed fractions
<ul> <li>Uses multiplication strategies to explain computation (e.g., doubles, 9- patterns, decomposing, partial products)</li> </ul>	Adds fractions with like denominators with reducing or converting to a mixed fraction	Uses models to multiply and divide fractions and mixed fractions and connect the actions to algorithms
<ul> <li>Multiplies a 3-digit number by a 3-digit number</li> </ul>	Adds fractions with unlike denominators without reducing	Divides a fraction by a fraction
<ul> <li>Multiplies a 4- or more digit number by multiples of 100 or 1000</li> </ul>	Adds fractions with unlike denominators with reducing or converting to	Divides a fraction by a whole number
<ul> <li>Multiplies multiple-digit numbers</li> </ul>	a mixed fraction	Divides a whole number by a fraction
<ul> <li>Models whole number multiplication and division algorithms (e.g., uses physical materials to show 4 groups of 3 objects)</li> </ul>	Adds simple mixed fractions with unlike denominators (e.g., halves, thirds, fourths, eighths)	Divides a mixed fraction by a whole number
Divides a 2-digit number or a 3-digit number by a 1-digit number with a	Adds mixed fractions where converting from improper fractions is	Divides a whole number by a mixed fraction
remainder	necessary	Divides a mixed fraction by a fraction
<ul> <li>Performs mental computation with division</li> </ul>	Subtracts fractions with like denominators with reducing	Divides a fraction by a mixed fraction
<ul> <li>Divides a 4-digit number by a 1-digit number with no remainder</li> </ul>	Subtracts fractions with unlike denominators without reducing	• Divides a mixed fraction by a mixed fraction
<ul> <li>Divides a 3-digit number by a 2-digit number</li> </ul>	Subtracts fractions with unlike denominators with reducing	Solves 2- or more step real-world problems involving fractions with multiplication and division
<ul> <li>Divides a 4-digit number by a 2-digit number</li> </ul>	Subtracts mixed fractions with unlike denominators with no regrouping	Solves problems involving fractions (e.g., multiple operations,
Divides multiple-digit numbers	Subtracts whole numbers, fractions, and mixed fractions	conversions)
<ul> <li>Solves whole number word problems with division over 10 x 10</li> </ul>	Subtracts whole numbers, fractions, and mixed fractions with regrouping	Subtracts a decimal from a whole number, horizontally
Solves complex word problems involving whole number division with     remainder (a.g., 2 stop, 2 digit divisor)	Solves real-world problems involving addition and subtraction of	Multiplies a decimal by 10, 100, 1000
remainder (e.g., 2-step, 2-digit divisor)	fractions where converting one denominator is necessary	Divides a whole number by a decimal
<ul> <li>Solves real-world problems involving 2-step multiple operations, whole numbers only</li> </ul>	Uses models to multiply and divide fractions and connect the actions	• Divides a decimal by 10, 100, 1000
Solves real-world multiple-step problems involving whole numbers	to algorithms	Divides a decimal by a decimal
Demonstrates an understanding of the inverse relationship between     addition and subtraction	• Multiplies a fraction by a fraction without reducing to simplest form (complex problem)	Adds integers with unlike signs     Adds several positive and possitive integers
Adds fractions with like denominators without reducing	Multiplies a fraction by a fraction where reducing to simplest form is	Adds several positive and negative integers     Subtracts integers
- Adds reactions with the denominators without readony	necessary	Solves problems involving addition and subtraction of integers
	Multiplies a fraction by a whole number	

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Perform Operations	Perform Operations	Perform Operations
Adds fractions with like denominators with reducing or converting to a	Multiplies mixed fractions	Multiplies integers with like signs
mixed fraction	Divides a fraction by a fraction	Divides integers with like signs
<ul> <li>Adds fractions with unlike denominators without reducing</li> </ul>	Divides a mixed fraction by a fraction	Subtracts rational expressions in decimal form
<ul> <li>Adds simple mixed fractions with unlike denominators (e.g., halves, thirds, fourths, eighths)</li> </ul>	Solves 1-step real-world problems involving fractions with multiplication and division	Multiplies rational expressions
<ul> <li>Subtracts simple fractions with unlike denominators without reducing (e.g., halves, quarters, thirds, eighths)</li> </ul>	Solves 2- or more step real-world problems involving fractions with multiplication and division	<ul><li>Identifies the additive inverse property</li><li>Interprets data given in tables to solve problems</li></ul>
<ul> <li>Subtracts fractions with unlike denominators without reducing</li> </ul>	Solves problems involving fractions (e.g., multiple operations,	Writes a fraction as a decimal and vice versa
Subtracts mixed fractions with like denominators with no regrouping	conversions)	Writes a fraction as a mixed decimal and vice versa
Subtracts mixed fractions with unlike denominators with no regrouping	Adds decimals to the hundredths place in horizontal format (not same	
Solves real-world problems involving addition and subtraction of	number of digits)	
fractions where converting one denominator is necessary	Adds decimals through the hundred-thousandths place	
Uses models to multiply and divide fractions and connect the actions to algorithms	Subtracts decimals to the hundredths place (not same number of digits)	
<ul> <li>Multiplies a fraction by a fraction where reducing to simplest form is necessary</li> </ul>	• Subtracts decimals to the thousandths place, horizontally, with and without regrouping	
<ul> <li>Multiplies a fraction by a whole number</li> </ul>	Subtracts decimals through the hundred-thousandths place,	
Solves 1-step real-world problems involving fractions with	horizontally	
multiplication and division	Subtracts a decimal from a whole number, horizontally	
<ul> <li>Adds decimals to the hundredths place in horizontal format (not same number of digits)</li> </ul>	• Multiplies a decimal by a decimal, vertical form (factors to tenths or hundredths)	
Adds decimals to the thousandths place horizontally with and without	<ul> <li>Multiplies a decimal by a decimal (factors to hundredths)</li> </ul>	
regrouping	Multiplies a decimal by 10, 100, 1000	
Adds decimals through the hundred-thousandths place	Multiplies a decimal by a decimal (factors to thousandths)	
<ul> <li>Subtracts decimals to the thousandths place, horizontally, with and without regrouping</li> </ul>	• Divides a decimal by 10, 100, 1000	
Computes the value of multiple bills and coins (addition/subtraction	Divides a decimal by a decimal	
only)	Computes with dollars and cents over \$5.00 and converts to decimals     (multiplication/division)	
<ul> <li>Analyzes and computes 1 operation on real-world problems involving money over \$5.00 (addition/subtraction only)</li> </ul>	Computes the value of multiple bills and coins (multiplication/division)	
• Multiplies a decimal by a decimal, vertical form (factors to tenths or	Calculate the sum of integers using a number line	
hundredths)	Adds integers with unlike signs	
Multiplies a decimal by a decimal (factors to hundredths)	Adds several positive and negative integers	
Divides decimal by a whole number	Uses models to add and subtract integers and connect the actions to algorithms	
<ul> <li>Analyzes and computes 1 operation on real-world problems involving money over \$5.00 (multiplication/division)</li> </ul>	Subtracts integers	
Computes with dollars and cents over \$5.00 and converts to decimals (multiplication/division)	Solves real-world problems involving addition and subtraction of integers	
Computes addition and subtraction on multiple-step real-world	Solves problems involving addition and subtraction of integers	
problems involving money	Multiplies integers with unlike signs	
	Divides integers with unlike signs	

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Perform Operations	Perform Operations	Perform Operations
<ul> <li>Computes addition, subtraction, multiplication, and division on multiple- step, real-world problems involving money</li> <li>Adds integers with like signs</li> <li>Uses models to add and subtract integers and connect the actions to algorithms</li> <li>Solves real-world problems involving addition and subtraction of integers</li> <li>Multiplies integers with unlike signs</li> <li>Divides integers with unlike signs</li> <li>Divides integers with unlike signs</li> <li>Demonstrates an understanding that division by 0 is undefined</li> <li>Solves difficult problems involving elapsed time, with the conversion of hours</li> <li>Selects and uses the appropriate units depending on degree of accuracy required to solve problems</li> <li>Expresses a simple fraction as a decimal</li> <li>Writes a fraction or mixed number as a decimal and vice versa</li> <li>Writes a fraction or mixed number as a decimal when the denominator is a multiple of 10</li> <li>Expresses the equivalent form of a fraction, decimal, and/or percent (simple fraction)</li> <li>Determines factors of whole numbers</li> <li>Identifies numbers as prime</li> <li>Identifies common factors of two or more numbers</li> </ul>	<ul> <li>Divides integers with like signs</li> <li>Adds rational expressions in decimal form</li> <li>Identifies the additive inverse property</li> <li>Solves difficult problems involving elapsed time, with the conversion of hours</li> <li>Interprets data given in tables to solve problems</li> <li>Writes a simple mixed fraction as a decimal and vice versa</li> <li>Writes a fraction or mixed number as a decimal when the denominator is a multiple of 10</li> <li>Determines factors of whole numbers</li> <li>Uses multiple number theory concepts to solve problems (e.g., factors, digits, odd/even, divisibility)</li> <li>Uses factor and multiple concepts to solve simple problems</li> <li>Identifies the greatest common factor of whole numbers</li> </ul>	
Identifies the greatest common factor of whole numbers  Extend and Use Properties	Extend and Use Properties	Extend and Use Properties
<ul> <li>Predicts the relative size of the answer when computing with 10's, 100's, 1000's</li> <li>Predicts the relative size of the answer when multiplying whole numbers</li> <li>Determines the distance between horizontal and vertical lines in the first quadrant of a rectangular coordinate system</li> <li>Locates the origin on a coordinate grid</li> <li>Rounds 4-, 5-, and 6-digit whole numbers to the nearest hundred</li> <li>Rounds 4-, 5-, and 6-digit whole numbers to the nearest thousand</li> <li>Rounds 4-, 5-, and 6-digit whole numbers to the nearest thousand</li> <li>Rounds 4-, 5-, and 6-digit whole numbers to the nearest ten thousand</li> </ul>	<ul> <li>Graphs ordered pairs in all quadrants</li> <li>Computes and interprets distance, given a set of ordered pairs (horizontal and vertical lines)</li> <li>Determines the relative magnitude of whole numbers</li> <li>Rounds whole numbers to the nearest million</li> <li>Writes equivalent forms of whole numbers using place value (numbers 100 or greater) (e.g., 253 = 2 hundreds, 5 tens, and 3 ones)</li> <li>Writes whole numbers in standard and exponential form</li> <li>Identifies a fractions in lowest terms from a region or set</li> <li>Determines simple equivalent fractions using multiples</li> <li>Determines equivalent fractions using multiples</li> <li>Compares fractions (e.g., comparing numerators and denominators)</li> </ul>	<ul> <li>Simplifies rational expressions with absolute value</li> <li>Graphs ordered pairs in all quadrants</li> <li>Computes and interprets distance, given a set of ordered pairs (horizontal and vertical lines)</li> <li>Determines the relative magnitude of whole numbers</li> <li>Writes whole numbers in standard and exponential form</li> <li>Compares fractions (e.g., comparing numerators and denominators)</li> <li>Rounds decimals to the nearest hundredth</li> <li>Compares and orders decimal and fractional coordinates on a number line</li> </ul>

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Extend and Use Properties	Extend and Use Properties	Extend and Use Properties
Writes whole numbers in standard and expanded form through the	<ul> <li>Uses alternative algorithms to explain the meaning of fraction</li> </ul>	
hundred thousands	• Represents a decimal to thousandths place (e.g., three thousandths =	
<ul> <li>Identifies equivalent fractions using visual representations</li> </ul>	0.003)	
<ul> <li>Identifies a fractions in lowest terms from a region or set</li> </ul>	• Represents a decimal to the hundred thousandths place - (e.g., three hundred thousandths = 0, 00002)	
<ul> <li>Identifies eighths, reduced to lowest terms, from a region or set</li> </ul>	hundred thousandths = 0. 00003)	
<ul> <li>Determines simple equivalent fractions using multiples</li> </ul>	Writes a decimal for a shaded region to the hundredths place	
<ul> <li>Converts fractions to lowest terms</li> </ul>	Compares and orders decimals to the hundredths place (not same number of digits after decimal)	
Writes mixed numbers as improper fractions and improper fractions as mixed numbers	Compares and orders decimals to the thousandths place (not same number of digits after decimal)	
<ul> <li>Compares fractions on a number line</li> </ul>	Compares and orders decimals past the thousandths place	
<ul> <li>Compares fractions greater than or less than a given fraction using</li> </ul>	Rounds decimals to the nearest hundredth	
visual representations		
<ul> <li>Compares fractions and mixed numbers</li> </ul>	Rounds decimals to nearest thousandth	
<ul> <li>Compares fractions and mixed numbers using symbols</li> </ul>	<ul> <li>Identifies the place value and value of each digit to the hundredths and thousandths</li> </ul>	
<ul> <li>Orders fractions on a number line</li> </ul>	Applies base ten place value concepts to solve problems using	
<ul> <li>Explains different interpretations of fractions (e.g., parts of a whole, parts of a set, and division of whole numbers by whole numbers)</li> </ul>	decimals	
• Represents a decimal to the hundredths place (e.g., three hundredths	Compares two integers	
= 0.03)	Orders integers on a number line	
<ul> <li>Compares and orders decimals past the thousandths place</li> </ul>	Orders integers	
<ul> <li>Rounds decimals to the nearest whole number</li> </ul>	<ul> <li>Locates rational numbers on a number line</li> </ul>	
<ul> <li>Rounds decimals to the nearest tenth</li> </ul>	<ul> <li>Orders rational numbers, in a/b form</li> </ul>	
<ul> <li>Applies base ten place value concepts to solve problems using decimals</li> </ul>	Orders fractions and decimals to the hundred thousandths	
<ul> <li>Identifies an integer from a number line</li> </ul>		
Compares two integers		
Orders integers on a number line		
Defines integers		
New Vocabulary: century, coin, common factor, decimal form, greatest common factor, how long, lowest term, lowest terms, reduce, triple	New Vocabulary: real number, ten million New Signs and Symbols: () parenthesis around an integer, cm	New Vocabulary: discount, equality New Signs and Symbols:    absolute value, oz ounce
New Signs and Symbols: \$ dollar sign, hr hour, kg kilogram, - negative sign, ≠ not equal to, yd yard	centimeter/centimetre, °C degrees Celsius, km kilometer/kilometre, mL milliliter/millilitre, # number, / per, + positive number, : ratio	I vew Signs and Symbols.    absolute value, oz ounce

### **Explanatory Notes**